

# Must Know Material for FINAL - M151 - Calculus II - Spring 2021

The following is a comprehensive list of the topics that will (and will not) be included in the final:

- Sec. 3.11 Hyperbolic Functions
- Sec. 6.1: Areas Between Curves
- Sec. 6.2: Volumes (by slices, disks and washers)
- Sec. 6.3: Volumes by Cylindrical Shells
- Secs. 6.4 and 6.5 will **NOT** be included in Final
- Sec. 7.1: Integration by Parts
- Sec. 7.2: Trigonometric Integrals
- Sec. 7.3: Trigonometric Substitution
- Sec. 7.4: Partial Fractions
- Sec. 7.8: Improper Integrals
- Sec. 8.1: Arc Length
- Sec. 8.2: Surface of Revolution
- Sec. 9.3: Separable Equations (**NO** orthogonal curves and **NO** mixing problems)
- Sec. 9.5: Linear Differential Equations
- Sec. 11.2: Series (only geometric series and its applications)
- Sec. 11.6: Ratio Test: interval and radius of convergence (**NO** absolute convergence and **NO** Root test)
- Sec. 11.9: Representations of Functions as Power Series
- Sec. 11.10: Taylor and Maclaurin Series (**NO** Taylor inequality and **NO** remainder)
- Sec. 11.11: Applications of Taylor Series (**only** Approximating Functions by Polynomials, **NO** Remainder)
- Sec. 10.1: Curves Defined by Parametric Equations
- Sec. 10.2: Calculus with parametric Equations
- Sec. 10.3: Polar Coordinates (inc. slopes that was not included in MiniTest#4)
- Sec. 10.4: Areas and Lengths in Polar Coordinates (this material was not included in MiniTest#4)
- Secs. 10.5 and 10.6 will **NOT** be included in Final

You must also be very confident with **ALL** the material covered in previous Mini-tests. You can have a look at the following “Must-know material for previous Mini-Tests”:

- [http://carretero.sdsu.edu/teaching/M-151/MTs/MiniTest1\\_must\\_know.pdf](http://carretero.sdsu.edu/teaching/M-151/MTs/MiniTest1_must_know.pdf)
- [http://carretero.sdsu.edu/teaching/M-151/MTs/MiniTest2\\_must\\_know.pdf](http://carretero.sdsu.edu/teaching/M-151/MTs/MiniTest2_must_know.pdf)
- [http://carretero.sdsu.edu/teaching/M-151/MTs/MiniTest3\\_must\\_know.pdf](http://carretero.sdsu.edu/teaching/M-151/MTs/MiniTest3_must_know.pdf)
- [http://carretero.sdsu.edu/teaching/M-151/MTs/MiniTest4\\_must\\_know.pdf](http://carretero.sdsu.edu/teaching/M-151/MTs/MiniTest4_must_know.pdf)

In addition to studying **ALL** Calc-I and Calc-II material above, you must be very confident with the following basic and fundamental topics/formulas/techniques/tricks/hints/etc.:

## SEQUENCES and SERIES:

- Geometric series.
- Applications of geometric series: problems involving: investments, savings, interests, loans, drug delivery, fractals, bounding balls, etc... (check textbook/HWs/labs/worksheets for all different types of problems).
- Computing interval and radius of convergence (using ratio test).
- Taylor and McLaurin series (no Taylor inequality and no remainder).
- Remember that  $n! = 1 \times 2 \times \cdots \times n$ , that  $(n + 1)! = (n + 1) \times n!$ , and that  $0! = 1$  and  $1! = 1$ .

In addition to **ALL** the material that was included in the MiniTests, you must be **VERY** confident with the following basic and fundamental topics/techniques/etc. that were not covered in the MiniTests:

- Polar coordinates:  $r = f(\theta)$ 
  - Tangent’s slope in polar: use tangent for parametric (as above) with  $x = f(\theta) \cos(\theta)$  and  $y = f(\theta) \sin(\theta)$ :
    - \* Horizontal  $\Rightarrow m=0/\text{const}$  (i.e. numerator of  $m(\theta) = 0$  **and** denominator  $\neq 0$ ).
    - \* Vertical  $\Rightarrow m=\text{const}/0$  (i.e. denominator of  $m(\theta) = 0$  **and** numerator  $\neq 0$ ).
    - \*  $0/0$  or  $\infty/\infty \Rightarrow$  L’Hôpital (i.e. **both** numerator and denominator are zero or both are  $\pm\infty$ ).
    - \* Point-slope formula:  $(y - y_0) = m(x - x_0)$ .
  - Area:  $A = \int_{\theta_1}^{\theta_2} \frac{1}{2} [f(\theta)]^2 d\theta$ .
  - Arclength:  $L = \int_{\theta_1}^{\theta_2} \sqrt{[f(\theta)]^2 + [f'(\theta)]^2} d\theta$ .